# Excess enthalpies for binary mixtures of toluene, *p*-xylene or pseudocumene + methyl-*n*-alkyl ketones. Application of an extended cell model

Romolo Francesconi<sup>a,\*</sup> and Fabio Comelli<sup>b</sup>

<sup>a</sup> Dipartimento di Chimica 'G. Ciamician', Università degli Studi, via Selmi 2, I-40126 Bologna (Italy) <sup>b</sup> Centro'di Studio par la Fisica delle Macromolecole del C.N.R., via Selmi 2, I-40126 Bologna (Italy) (Received 12 June 1992)

Abstract

Excess molar enthalpies  $H^{E}$  of the fifteen binary mixtures containing toluene, *p*-xylene or pseudocumene + five methyl-*n*-alkyl ketones at 298.15 K and atmospheric pressure are reported. The results confirm for *p*-xylene or pseudocumene + ketones the systematic behavior of  $H^{E}$  with respect to the chain length of the ketone, whereas for the toluene + 2-undecanone mixture, an inversion in the tendency of  $H^{E}$  has been noted (Patterson effect). The experimental data are examined by an extended cell model.

## INTRODUCTION

This work was undertaken as part of a long program to provide accurate experimental information about the changes in the thermodynamic properties of a binary mixture which result from increased chain lengths in the molecular configuration of one of its components. For this purpose five methyl-*n*-alkyl ketones, namely 2-propanone, 2-butanone, 2-pentanone, 2-octanone and 2-undecanone, were taken into consideration.

Previous papers [1-3] report excess molar enthalpies  $H^{\rm E}$  for the binary mixtures of the above ketones with halothane or naphthalene derivatives. Continuing this study, we have determined excess molar enthalpies for binary mixtures of three methyl-substituted benzene compounds, namely toluene, *p*-xylene and pseudocumene (1,2,4-trimethylbenzene) with the same ketones over the whole composition range, at atmospheric pressure and 298.15 K.

To our knowledge, excess enthalpy data for these fifteen binary systems have not previously been reported.

<sup>\*</sup> Corresponding author.

## EXPERIMENTAL

## Apparatus

Molar excess enthalpies  $H^{E}$  were obtained by using an LKB flow microcalorimeter (Model 2107, Produkter AB, Bromma, Sweden). Fully automatic burets (ABU, Radiometer, Copenhagen, Denmark) were used to pump the pure liquids into the mixing cell. Details of the equipment and its operation have been described previously [4, 5]. Calibration was checked by determining the  $H^{E}$  at 298.15 K for the test system cyclohexane-hexane over the whole composition range. The agreement with the literature [6] is better than 0.5% over the central range of concentration.

## Chemicals

Sources of the liquid compounds and purities specified by the manufacturers are summarized in Table 1. Liquids were used without further purification (stated purity  $\geq$ 99%) with the exception of 2-octanone, which was distilled following the method of Collerson et al. [7]. Before use, liquids were stored in dark bottles over molecular sieves (Union Carbide, type 4A, 1/16 inch pellets).

## Density measurements

Densities of pure compounds, also required for evaluating fluxes and, hence, mole fractions in the calorimetric measurements, were determined

#### TABLE 1

Sources, purities and densities (T = 298.15 K) of liquid compounds and comparison with literature data

Liquid	Source and Purity	$ ho (\mathrm{g}\mathrm{cm}^{-3})$			
		Obsd.	Lit.		
Toluene	Aldrich, Research Grade 99.9%	0.862149	0.86219 [8]		
<i>p</i> -Xylene	Aldrich, Research Grade 99.5%	0.856620	0.85661 [8]		
Pseudocumene	Kodak, Research Grade 99%	0.871963	0.87180 [9]		
2-Propanone	Aldrich, Research Grade 99.9+%	0.785005	0.7844 [8]		
2-Butanone	Aldrich, Research Grade 99.5+%	0.799905	0.7997 [8]		
2-Pentanone	Fluka, Research Grade 99+%	0.801400	0.8015 [8]		
2-Octanone	Aldrich, Research Grade 98%	0.814359	0.8143 [8]		
2-Undecanone	Aldrich, Research Grade 99%	0.821704	0.8221 [10]		

at 298.15  $\pm$  0.01 K in a digital density meter (Anton Paar DMA 60/602) and are listed in Table 1, with values from the literature [8–10] for comparison. The density meter, described elsewhere [11], was thermostated by a Colora constant temperature bath circulator with a temperature control interval of  $\pm$ 0.01 K. The temperature was detected with a digital thermometer (Anton Paar DT 100-25) and the precision of the densities measured is estimated to be of the order of  $1 \times 10^{-6}$  g cm<sup>-3</sup>.

## CORRELATION OF THE CALORIMETRIC DATA

The experimental values of  $H^{E}$  are given in Table 2 and shown graphically in Figs. 1–3.

In all cases,  $x_1$  denotes the mole fraction of toluene, *p*-xylene or pseudocumene in the mixture. The Redlich-Kister polynomial equation

$$H^{\rm E}/x_1x_2 = \sum_{k=0}^{n-1} a_k (x_1 - x_2)^k \tag{1}$$

with *n* the number of the adjustable parameters  $a_k$ , was fitted to each set of data by the method of least-squares, with all points weighted equally; parameters  $a_k$  based on the lowest values of standard deviation

$$\sigma(H^{\rm E}) = [\phi/(N-n)]^{0.5} \tag{2}$$

are listed in Table 3;  $\phi$  is the objective function defined as

$$\phi = \sum_{k=1}^{N} \eta_k^2 \tag{3}$$

with N the number of experimental points,  $\eta_k = H_{calc}^E - H^E$ ;  $H_{calc}^E$  has been determined from the right-hand side of eqn. (1).

The number of parameters of Table 3 corresponds to values of  $\sigma(H^{\rm E})$  comparing with the mean uncertainty in the experimental  $H^{\rm E}$  calculated following the procedure given in ref. 4.

Figure 4 shows the correlation between the values of  $H^{\rm E}$  for  $x_1 = 0.5$  and  $n_{\rm c}$ , the number of carbon atoms in the linear methyl-alkyl ketones.

#### THE CELL MODEL

A thermodynamic description of the curves in Figs. 1–3 has been attempted on the basis of an extended cell model worked out by Prigogine et al. [12–14], Salsburg and Kirkwood [15] and Rowlinson [16, 17].

## TABLE 2

Experimental molar excess enthalpies  $H^{E}$  of toluene, *p*-xylene or pseudocumene + methyl*n*-alkyl ketone mixtures at 298.15 K

Toluene + 2-propanone $0.0280$ $21.8$ $0.3158$ $200.9$ $0.7347$ $21.8$ $0.0545$ $40.9$ $0.4091$ $226.0$ $0.8060$ $14.9$ $0.1034$ $81.1$ $0.5095$ $243.8$ $0.8470$ $11.9$ $0.1875$ $134.8$ $0.5806$ $242.3$ $0.8925$ $14.9$ $0.2571$ $172.8$ $0.6750$ $221.9$ $0.9432$ $31.9$ $0.0340$ $-1.0$ $0.3602$ $15.1$ $0.8352$ $0.0657$ $0.0657$ $-1.8$ $0.4578$ $28.0$ $0.8711$ $31.9$ $0.1234$ $-1.7$ $0.5588$ $43.6$ $0.9102$ $41.966$ $0.1743$ $0.1$ $0.6281$ $53.9$ $0.9530$ $31.96643$ $31.96643$ $0.2969$ $8.2$ $0.7716$ $66.4$ $66.4$ $71.43.3$ $0.8009$ $-31.96643$ $31.966643$ $31.966643$ $31.9666644$ $31.966643$ $31.9666644$ $31.9666644$ $31.9666644$ $31.966643$ $31.9666644$ $31.9666644$ $31.96666444$ <td< th=""><th></th></td<>	
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Toluene + 2-butanone $0.0340$ $-1.0$ $0.3602$ $15.1$ $0.8352$ $0.0657$ $-1.8$ $0.4578$ $28.0$ $0.8711$ $30.012$ $0.1234$ $-1.7$ $0.5588$ $43.6$ $0.9102$ $30.012$ $0.1743$ $0.1$ $0.6281$ $53.9$ $0.9530$ $30.02969$ $0.2969$ $8.2$ $0.7716$ $66.4$ $66.4$ Toluene + 2-pentanone $0.0773$ $-28.2$ $0.5014$ $-114.3$ $0.8009$ $-30.029678$	56.1
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	)1.9 )2.0
0.1450 - 52.7 0.0014 - 101.9 0.0576	32.8
0.2510 - 87.1 0.6679 - 87.5 0.9235	13.6
0.3346 -108.0 0.7511 -65.3 0.9602 -	-5.7
0.4014 -113.8	
Toluene + 2-octanone	
0.0578 - 24.5 0.4242 - 130.4 0.8155 - 3	55.7
0.1093 -46.0 0.4955 -131.6 0.8551 -2	39.8
0.1971 -81.9 0.5956 -121.0 0.8984 -2	23.0
0.2692 -104.3 0.6884 -99.8 0.9465 -	-9.2
0.3293 -118.4 0.7466 -79.4 0.9725 -	-3.0
Toluene + 2-undecanone	
0.0748 -23.0 0.4923 -95.1 0.7950 -4	42.1
0.1391 -41.8 0.5639 -91.2 0.8533 -2	27.1
0.244367.8 0.6598 -75.8 0.9209 -	-9.8
0.3266 -83.5 0.7442 -55.4 0.9588 -	-1.4
0.3927 -92.3	
p-Xylene + 2-propanone	
0.0474 64.5 0.3738 363.1 0.7817 24	30.9
0.0905 126.8 0.4725 387.3 0.8269 24	40.6
0.1660 216.3 0.5442 387.3 0.8775 18	34.6
0.2299 276.4 0.6417 365.6 0.9347 10	)6.6
0.2847 315.6 0.7048 337.0 0.9502	84.1
p-Xvlene + 2-butanone	
0.0572 17.1 0.3268 104.0 0.7444 1	49.2
0.1082 35.0 0.4214 126.8 0.8137 1	31.2
0.1540 50.1 0.5221 147.6 0.8535 1	13.1
0.1953 64.0 0.5929 156.6 0.8973	39.2
0.2669 85.9 0.6860 157.6 0.9459	53.5

<i>x</i> <sub>1</sub>	$H^{\mathrm{E}}(\mathrm{J} \mathrm{mol}^{-1})$	<i>x</i> <sub>1</sub>	$H^{\mathrm{E}}$ (J mol <sup>-1</sup>	') x <sub>1</sub>	$H^{\mathrm{E}}$ (J mol <sup>-1</sup> )
p-Xylene	+2-pentanone				
0.0674	-21.5	0.3663	-74.9	0.7762	-24.7
0.1263	-38.6	0.4644	-74.4	0.8388	-12.3
0.1782	-50.4	0.5655	-63.3	0.9123	-3.1
0.2242	-59.5	0.6343	-51.3	0.9542	-0.3
0.3025	-70.5	0.7223	-36.3		
p-Xylene	+2-octanone				
0.0503	-29.7	0.3884	-191.0	0.7921	-109.8
0.0957	-57.3	0.4585	-199.2	0.8358	-84.5
0.1747	-107.4	0.5595	-194.2	0.8840	-57.4
0.2410	-144.2	0.6558	-170.7	0.9384	-26.9
0.2975	-165.2	0.7176	-146.6	0.9682	-13.2
p-Xylene	+2-undecanone				
0.0651	-43.8	0.4554	-234.6	0.8338	-129.3
0.1223	-80.2	0.5272	-236.6	0.8702	-102.8
0.2180	-142.9	0.6258	-230.0	0.9094	-70.2
0.2949	-184.5	0.7150	-200.7	0.9525	-38.4
0.3579	-211.3	0.7698	-168.8		
Pseudocu	imene + 2-propanone				
0.0428	75.5	0.3493	417.4	0.7631	255.1
0.0821	136.2	0.4461	436.0	0.8111	214.4
0.1518	238.0	0.5177	423.2	0.8656	159.1
0.2116	306.7	0.6169	374.0	0.9280	86.7
0.2635	363.0	0.6822	324.4	0.9450	71.1
Pseudocu	mene + 2-butanone				
0.0546	43.3	0.3039	194.6	0.7237	208.3
0.0984	75.4	0.3957	228.4	0.7971	169.8
0.1407	102.6	0.4955	245.8	0.8871	103.8
0.1791	130.2	0.5670	249.0	0.9402	56.8
0.2466	168.6	0.6627	233.1	0.0	0010
Pseudocu	imene + 2-pentanone				
0.0610	-0.5	0.5392	-18.0	0.8618	-50.8
0.1150	-2.0	0.6093	-24.1	0.9034	-46.7
0.2063	-3.4	0.7005	-35.2	0.9258	-41.4
0.2805	-6.0	0.7572	-42.6	0.9493	-32.4
0.4381	-10.7	0.8239	-50.0	0.9615	-26.5
Pseudocu	imene + 2-octanone				
0.0454	-31.1	0.3635	-170.8	0.7741	-130.4
0.0869	-56.2	0.4323	-181.9	0.8207	-105.4
0.1599	-98.4	0.5332	-189.6	0.8727	-81.5
0.2221	-129.6	0.6315	-169.8	0.9320	-47.3
0.2757	-144.5	0.6956	-157.4	0.9648	-25.3
Pseudocu	mene + 2-undecanon	e			
0.0590	-46.8	0.4292	-243.9	0.8186	-162.3
0.1113	-83.3	0.5007	-253.3	0.8577	-131.0
0.2004	-146.2	0.6006	-249.6	0.9002	-101.2
0.2732	-188.5	0.6928	-225.3	0.9475	-58.3
0.3339	-215.4	0.7505	-200.7	0.9730	-32.2

TABLE 2 (continued)



Fig. 1. Comparison between Redlich-Kister fit (----) and cell model (---) for  $H^{E}$  at 298.15 K for toluene: +2-propanone (a); +2-butanone (b); +2-pentanone (c); +2-octanone (d); +2-undecanone (e); ( $\bullet$ ) experimental points.



Fig. 2. Comparison between Redlich-Kister fit (---) and cell model (---) for  $H^E$  at 298.15 K for *p*-xylene: +2-propanone (a); +2-butanone (b); +2-pentanone (c); +2-octanone (d); +2-undecanone (e); ( $\bullet$ ) experimental points.



Fig. 3. Comparison between Redlich-Kister fit (----) and cell model (---) for  $H^{E}$  at 298.15 K for pseudocumene: +2-propanone (a); +2-butanone (b); +2-pentanone (c); +2-octanone (d); +2-undecanone (e); ( $\bullet$ ) experimental points.

The theoretical expression for  $H^{E}$  given by this model and reported in ref. 14 is

$$H^{E} = x_{1}x_{2}E_{11}z[-1.44\theta + 10.76(RT/zE_{11})^{2} \times (-2\theta - \delta^{2} + 4\delta\theta x_{2} + 4x_{1}x_{2}\theta^{2})]$$
(4)

where z is the number of nearest neighbors in the quasi-lattice model

$$\delta = (E_{22} - E_{11})/E_{11} \tag{5}$$

$$\theta = [E_{12} - (E_{11} + E_{22})/2]/E_{11} \tag{6}$$

 $E_{kk}$  = intermolecular energy between identical molecules kk and  $E_{12}$  = intermolecular energy between dissimilar molecules.

Equation (4) has been applied to other binary systems [18, 19] and good agreement between calculated and experimental  $H^{E}$  values has been obtained. Calculation of  $H^{E}$  by eqn. (4) for the mixtures in this paper has

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Redlich-Kister	constants	$a_k$	and	standard	deviation	$\sigma$	of	the	molar	excess	enthalpy
according to equ	n. (1)										

Mixture	$a_0$ (J mol <sup>-1</sup> )	$a_1$ (J mol <sup>-1</sup> )	$a_2$ (J mol <sup>-1</sup> )	$a_3$ (J mol <sup>-1</sup> )	$a_4$ (J mol <sup>-1</sup> )	$\sigma (J \text{ mol}^{-1})$
Toluene						
+2-propanone	969.2	137.3				1.6
+2-butanone	137.6	313.5	206.2	74.1		0.4
+2-pentanone	-463.1	114.8	229.1			1.3
+2-octanone	-534.2	69.4	264.8	109.4		1.5
+2-undecanone	-382.3	46.0	215.7	117.8		1.1
<i>p</i> -Xylene						
+2-propanone	1564.2	108.4	105.7			2.9
+2-butanone	580.3	373.7	126.1			1.3
+2-pentanone	-284.2	183.6	136.7			0.6
+2-octanone	-809.5	84.0	312.4			2.0
+2-undecanone	-963.8	-95.9	229.8			2.4
Pseudocumene						
+2-propanone	1701.4	-504.2	-181.4	311.4		3.0
+2-butanone	992.8	126.3	-81.4			2.0
+2-pentanone	-58.0	-127.2	-239.0	-295.5	-140.0	0.5
+2-octanone	-739.8	-7.7				2.0
+2-undecanone	-1005.5	-150.5				2.6

been carried out following the procedure outlined in ref. 18. Essentially,  $\theta$  is adjusted so that the experimental  $H^{\rm E}(x_1 = 0.5)$  equals the value calculated by the righthand side of eqn. (4).  $E_{11}$  and  $E_{22}$  are evaluated from the heats of vaporization of the pure components. No relevant difference has been achieved by giving z values from 8 to 12.

## **RESULTS AND DISCUSSION**

As can be seen from Figs. 1-3, the cell model gives a good description of the calorimetric data of the present paper except for the mixtures toluene-butanone, *p*-xylene-pentanone and pseudocumene-pentanone, which show markedly asymmetric curves. Equation (6) may be used to obtain values of  $E_{12}$  which may be compared with the arithmetic mean  $E_m$  and the geometric mean  $E_g$  of the interaction energies  $E_{11}$  and  $E_{22}$ .

The binary mixtures of toluene, *p*-xylene or pseudocumene with the three longer-chained ketones have  $E_{12}$  values very close to  $E_m$  and consistently display negative  $H^E$  values, in agreement with the limiting case  $E_{12} = E_m$  treated in ref. 14.

The mixture toluene-butanone gives  $E_{12} \approx E_g$ , in agreement with positive  $H^E$  [14]; the other mixtures showing positive  $H^E$  have  $E_{12}$  in the range  $E_g \leq E_{12} \leq E_m$ .

Figures 1-3 show positive values of  $H^{E}$  for the binary mixtures of toluene, *p*-xylene or pseudocumene with acetone and butanone. The other mixtures have negative  $H^{E}$ . *p*-Xylene and pseudocumene in mixtures with ketones display a trend towards less positive  $H^{E}$  values as a function of



Fig. 4. Values of  $H_{0.5}^{E} = H^{E}(x_{1} = 0.5)$  at 298.15 K as a function of  $n_{c}$  for the binary mixtures of methyl-*n*-alkyl ketones: +toluene ( $\bullet$ ); +*p*-xylene ( $\blacksquare$ ); +pseudocumene ( $\blacktriangle$ ).

increased ketone chain length. This behavior is probably due to the fact that increasing the chain length of the ketone induces more polarization to the C=O group, giving rise to a stronger interaction with the electrons of the aromatic ring. This produces a larger value of  $E_{12}$  and a smaller value of  $H^{\rm E}$ , which is approximately proportional to  $E_{11} + E_{22} - 2E_{12}$ .

However, the mixture toluene-undecanone contradicts this behavior, because this curve shows values of  $H^{E}$  more positive than pentanone and octanone. Here the Patterson effect [20] seems to overcome the inductive effect of chain length.

The same conclusions can better be seen in Fig. 4, showing values of  $H^{E}(x_{1} = 0.5)$  as a function of the number  $n_{c}$  of C atoms in ketones.

Similar results have been observed for other binary mixtures containing methyl-alkly ketones, e.g. with halothane [1] or 1-methylnaphthalene [3] as the second component, (although the mixtures with halothane show curves overlapping and intersecting each other, with consequent difficulty in drawing conclusions).

The mixtures cyclohexane + 2-propanone, +2-butanone, +2-pentanone and, +2-hexanone [21] also show an analogous trend.

Our next work will consider the determination of excess volumes  $V^{E}$  for the same mixtures as this paper, and the calculation of  $V^{E}$  by means of the cell model leading to eqn. (4).

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